

CSE 12:

Basic data structures and object-oriented design

Jacob Whitehill
jake@mplab.ucsd.edu

Lecture Thirteen
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Hash tables.

Recap of BSTs

- Binary search trees (BSTs) offer $O(\log n)$ time costs for **add/remove/find** operations by exploiting order relationships among data.
- They are also memory efficient, in that only as many nodes are allocated as elements are contained in the BST.
- However, by utilizing more *memory* (greater space complexity), we can achieve even *higher* performance (lower time complexity).
- **Hash tables** offer $O(1)$ time costs for **add/remove/find** operations by investing more memory in the underlying storage.

Finite “universe” of objects to store

- Suppose you were developing a database of UCSD students.
- You may wish to build a function that allows you to retrieve a student’s full record given their student ID:

```
class Student {  
    int _studentID; // 4 bytes long  
    String _firstName, _lastName;  
    String _address;  
    String _favoriteColor;  
}
```



- In this application, the *key* would be the student ID, and the *value* associated with the key would be the whole `Student` record.

Finite “universe” of objects to store

- In this application (and others), there may exist only a finite **universe** of possible keys values.
- For instance, a 4-byte integer can only store about 4 billion different values \Rightarrow 4 billion unique keys.
- Sometimes this finite set of keys is small enough that we can allocate an array big enough to give *every possible key its own slot*.
- In this case, we can make the “search” process for a particular key *trivial*:
 - We simply “jump” to the unique array index assigned to that key.
 - This takes only $O(1)$ time in the *worst-case*.

Finite “universe” of objects to store

- For example, in a UCSD student database application, we could allocate an array 4 billion elements long.
- Whenever we wished to find a particular student, we simply *jump* to that student’s correct slot using the student ID as the *index*.
- E.g., student with ID# 0000008192 would be stored at slot 0000008192.
- Search is *trivial* -- $O(1)$.

Key (student ID)	Value (reference to Student object)
...	...
0000008187	
0000008188	
0000008189	
0000008190	
0000008191	
0000008192	student
0000008193	
0000008194	
...	...

Finite “universe” of objects to store

- Similarly, when adding a student, we simply insert an entry at his/her *unique location* in the array:

```
Student other =  
    new Student(8188, ...);  
_container.add(other);
```

- Since student IDs are guaranteed to be unique, there is exactly *one* element that will ever reside at the index of the array.

Key (student ID)	Value (reference to Student object)
...	
0000008187	
0000008188	other
0000008189	
0000008190	
0000008191	
0000008192	student
0000008193	
0000008194	
...	...

Finite “universe” of objects to store

- Using the idea sketched above, we could implement a `StudentDatabase` with excellent **time costs**.

```
class StudentDatabase {
    Student[] _allPossibleStudents = new Student[4294967296];

    void add (Student s) { // O(1)
        int index = s._studentID;
        _allPossibleStudents[index] = s;
    }

    // Returns null if s is not in the database
    Student get (Student s) { // O(1)
        int index = s._studentID;
        return _allPossibleStudents[index];
    }

    void remove (Student s) { // O(1)
        int index = s._studentID;
        _allPossibleStudents[index] = null;
    }
}
```


Finite “universe” of objects to store

- However, the **space costs** of this data structure are enormous.

```
class StudentDatabase {
    Student[] _allPossibleStudents = new Student[4294967296];

    void add (Student s) { // O(1)
        int index = s._studentID;
        _allPossibleStudents[index] = s;
    }

    // Returns null if s is not in the database
    Student get (Student s) { // O(1)
        int index = s._studentID;
        return _allPossibleStudents[index];
    }

    void remove (Student s) { // O(1)
        int index = s._studentID;
        _allPossibleStudents[index] = null;
    }
}
```

Finite “universe” of objects to store

- Allocating 4 billion entries for a UCSD student database is extremely wasteful.
- The universe of keys is far larger than the number we expect to ever want to store.
- What if we decreased the size of the table from 4 billion entries to storing, say, just 100,000?
- 100,000 is still far higher than the actual number of UCSD students, so there should be plenty of space.

Finite “universe” of objects to store

- With an array of only 100,000 entries, each student ID would *no longer have its own unique array index* -- multiple student IDs would have to “share” an index.
- We call the “sharing” of an array index by 2 (or more) student IDs a **collision**.
- Whenever a collision occurs, we have to store the student object “somewhere else” (more later).
- However, if we’re clever about how we assign array indices to student IDs, then collisions will rarely occur.
- We can still achieve $O(1)$ add/find/remove time in the *average case*.

Hash tables

- This idea is called a “hash table.”
- A **hash table** consists of a large array of M “slots” (or “buckets”) to store the user’s data.
- A hash table also requires:
 1. Some way of converting from an object’s *key* into an *index* that specifies where that object should be stored.
 - This is called a *hash function*.
 2. A method of handling *collisions*.
- In order to ensure good performance, M must be bigger than N , the number of data the user will want to store.

Hash function

- A *hash function* maps an object's *key* into an array index, i.e., a number from $0..M-1$, where M is the number of entries in the hash table.
- Simple example:

```
int hashFunction (int studentID) {  
    return studentID % M;  
}
```
- The *modulus* operator `%` divides `studentID` by `M`, and then returns the *remainder*. Examples:

$$3 \% 10 = 3$$

$$107 \% 10 = 7$$

$$7 \% 4 = 3$$

$$16 \% 5 = 1$$

Hash function

- To be useful, a hash function must be *fast*.
- Its performance should not depend on the particular key.
- A hash function must also be *deterministic*:
 - Given the *same key*, it must *always* return the *same array index*.
 - (Otherwise, how would we find something we stored earlier?)

Hash function

- A “good” hash function should also be *uniform*:
 - Each “slot” i in the array should be equally likely to be chosen as any other slot j .
 - We certainly don’t want to map every possible key to the same array index!
 - Uniformity is important to ensure good performance.

Hash function

- For instance, if M is 100000, then $\text{studentID} \% 100000$ is simply the *last 5 digits* of the student ID, e.g.:
 - `student1` with Student ID 0000013012 would map to index 13012.
 - `student2` with Student ID 1234567890 would map to index 67890.
 - These *indices* specify *where* in the array the students are *stored*.

Key (student ID)	Value (reference to Student object)
...	
13011	
13012	<code>student1</code>
13013	
...	
67889	
67890	<code>student2</code>
67891	
67892	
...	...

Handling collisions

- Unfortunately, on occasion, there would be two (or more) `Student` objects who are “hashed” (mapped) into the same array slot.

```
studentID1 = 2200012345;  
studentID2 = 1926112345;  
hashTable.add(studentID1, student1);  
hashTable.add(studentID2, student2);
```

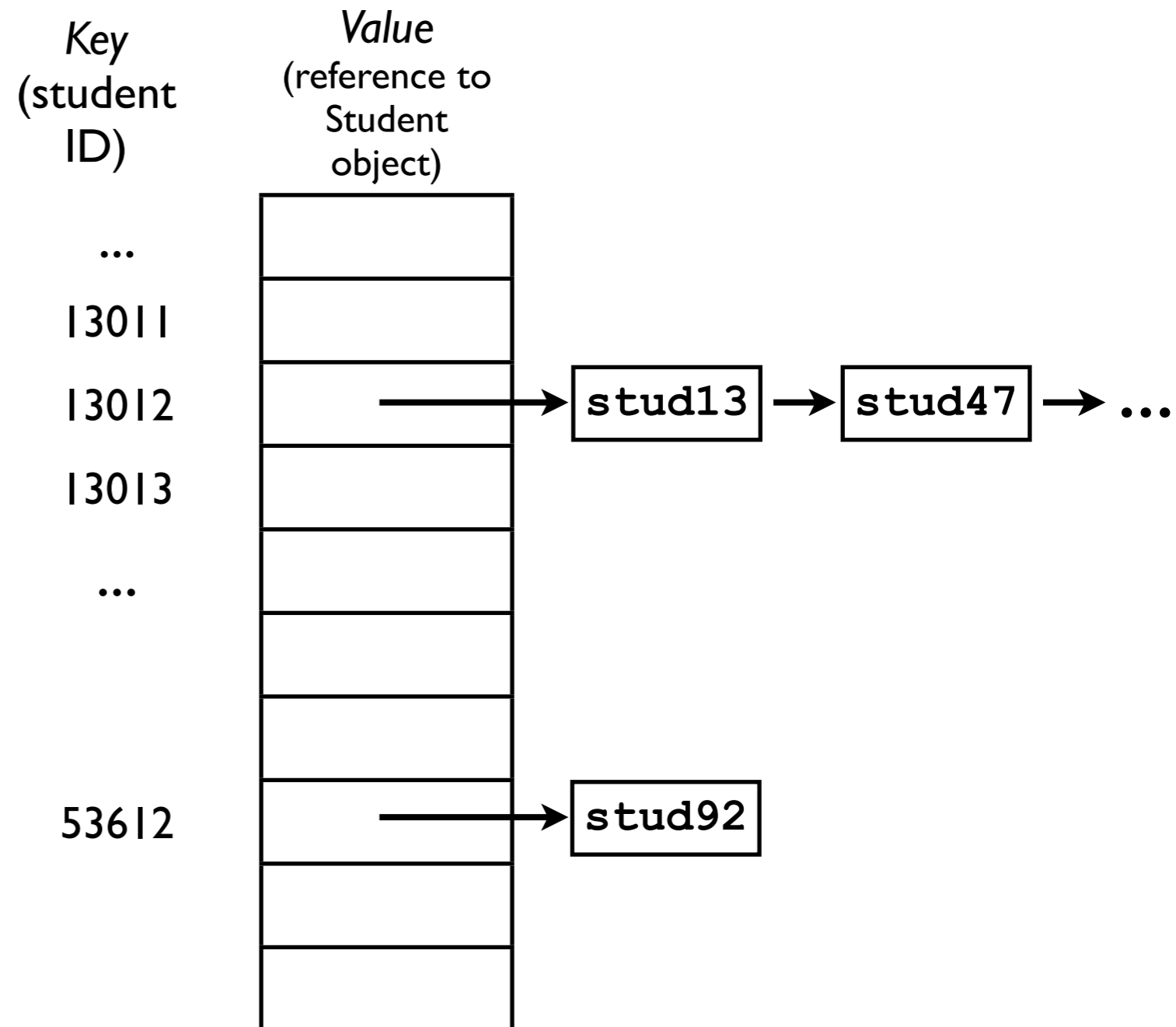
- This is called a *collision* -- two different `Student` objects map into the *same array index*.
- How do we handle these collisions?

Handling collisions

- There are two principal ways of handling collisions:
 1. **Chaining** (aka **separate chaining**) -- at each slot in the array, instead of storing only a single element, we store a linked list of elements.
 2. **Open addressing** -- if `student5` “hashes” to array index 123, and array index 123 is already occupied, then we look for “another” index at which to store `student5`, e.g., 124.
 - Different schemes for determining “another index”.

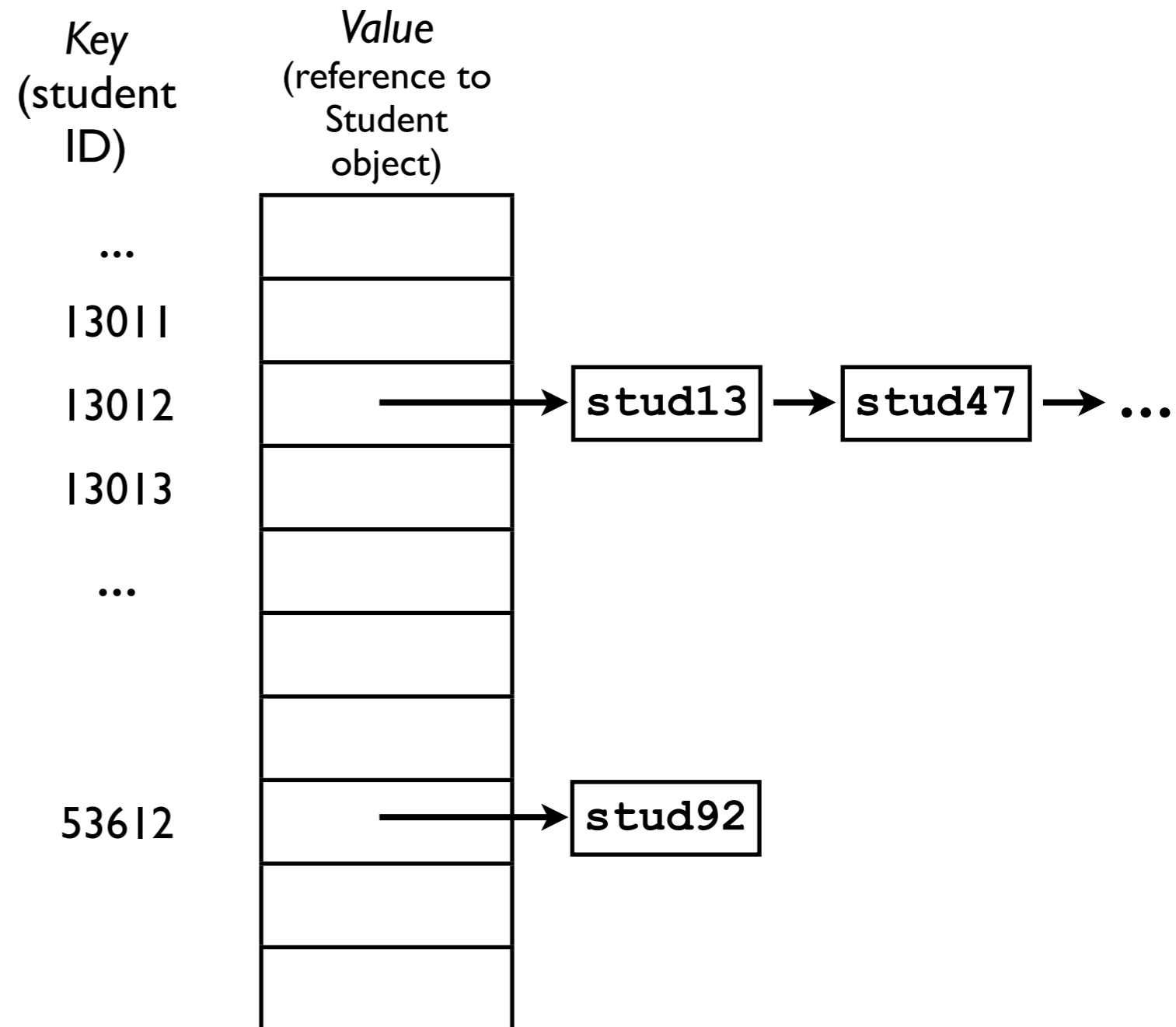
Chaining

- Each slot in the array contains not an object itself, but rather a pointer to the *head* of a *linked list* of objects which all map to the same index.



Chaining

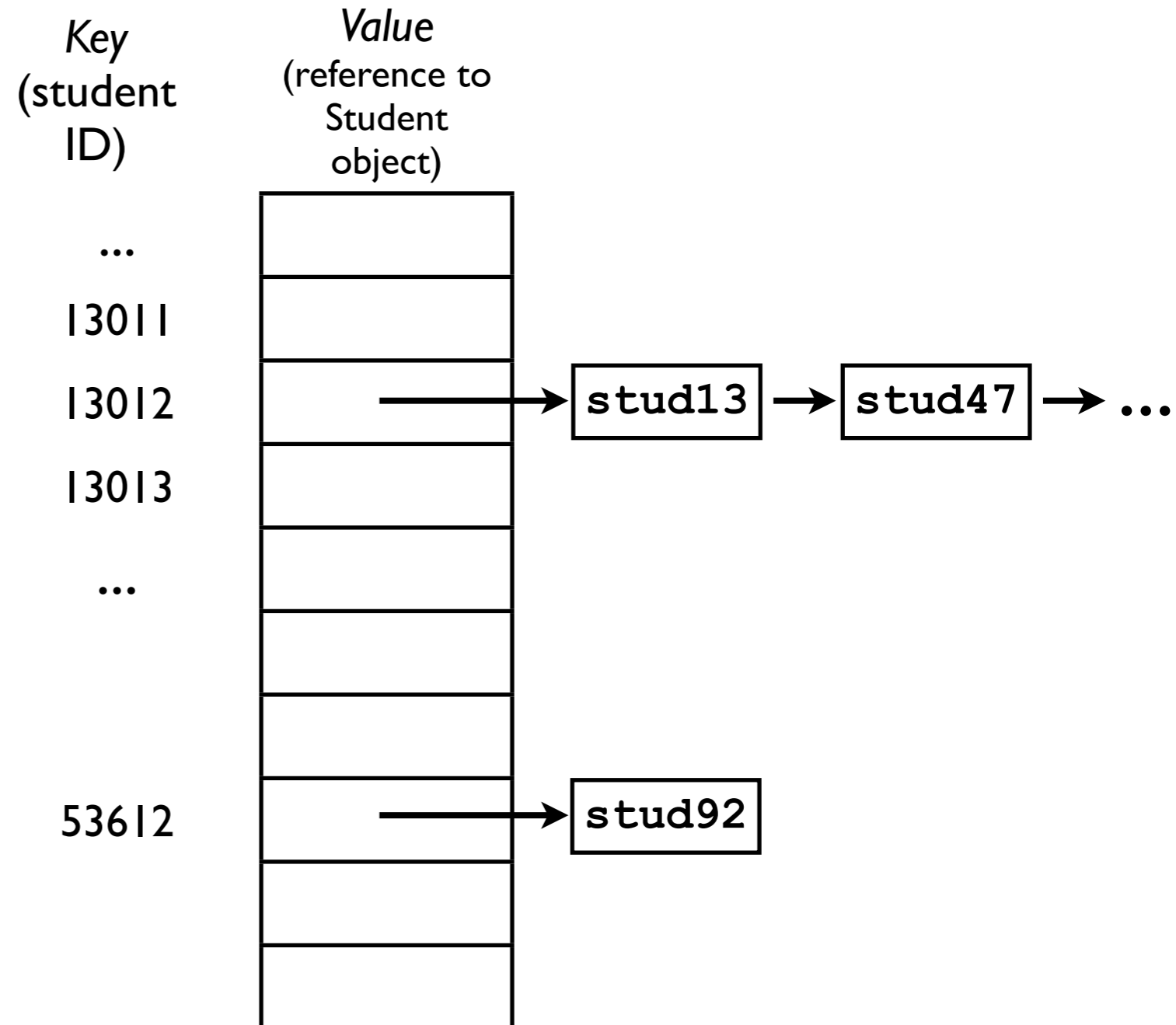
- When looking for a particular object, we must:
 1. *Hash* the key to obtain the *index*.
 2. *Search* the list for the correct object.
- This will still be *fast* as long as the linked lists are *short* (more later).



Chaining

- For example, if we wish to find `stud47` with student ID 0925113012.

1. Hash `stud47`'s student ID to determine the *index*.
2. Jump to the head of the corresponding linked list.
3. Traverse the linked list until we find `stud47`.



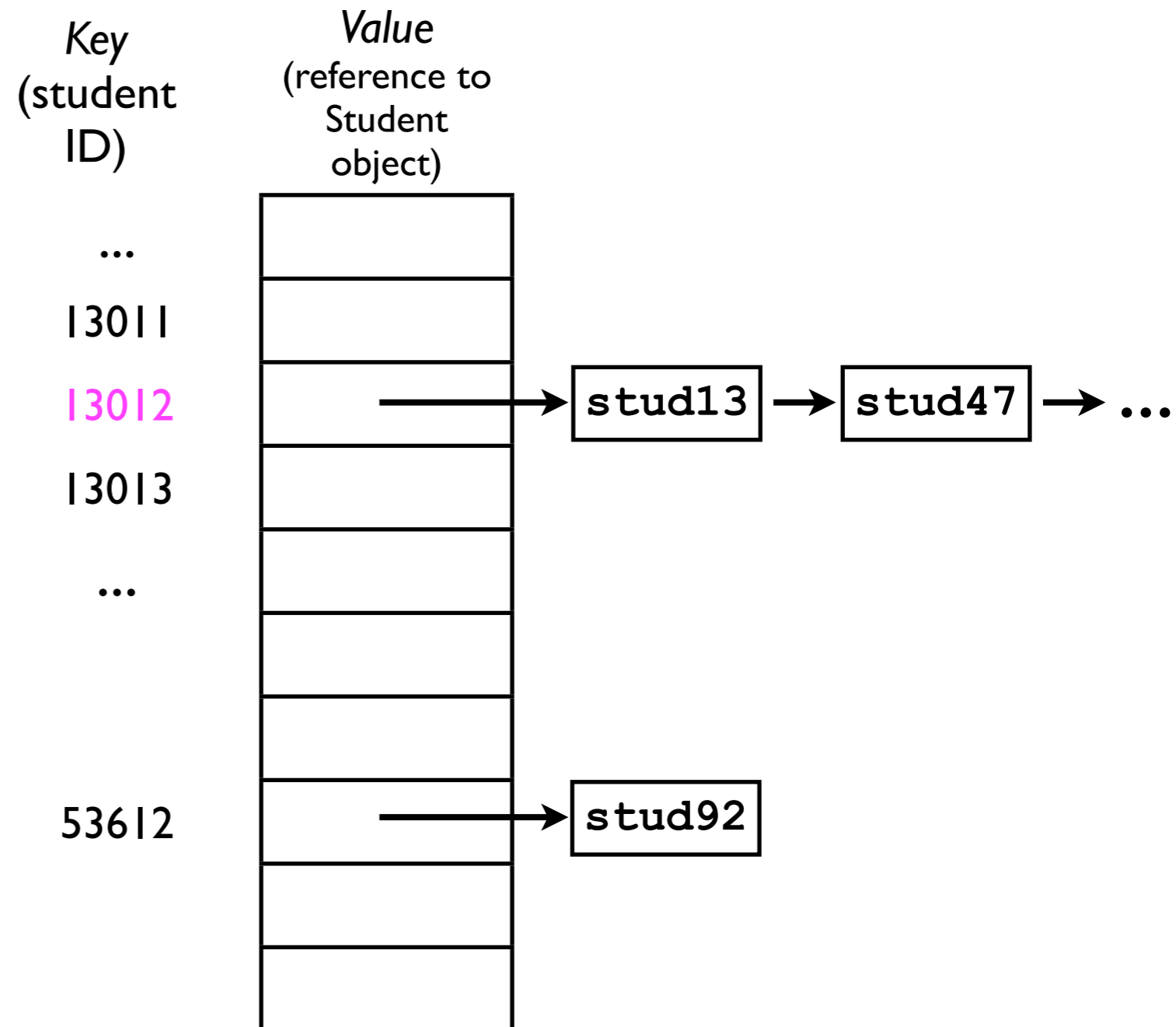
Chaining

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1. Hash `stud47`'s student ID to determine the *index*.

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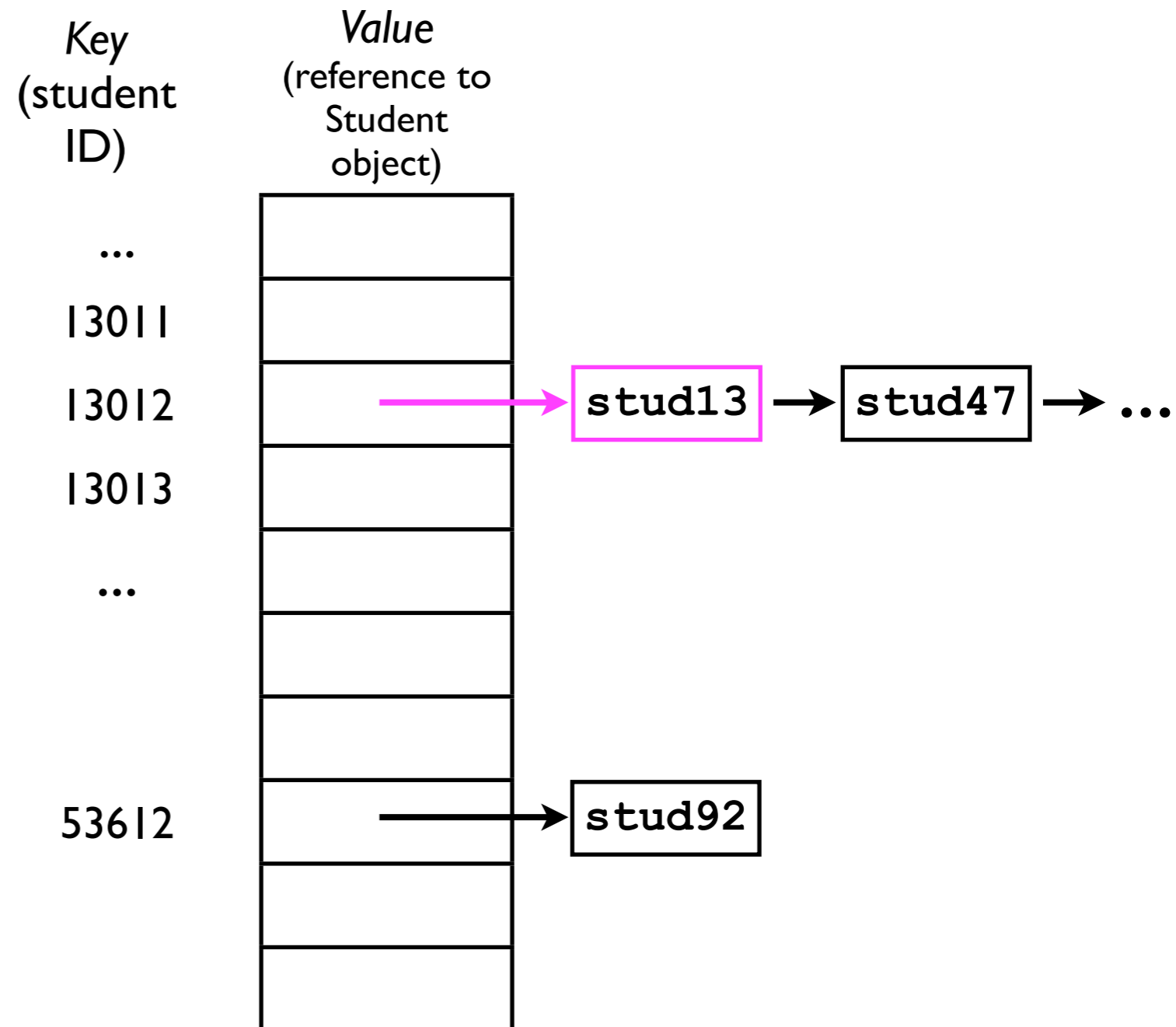
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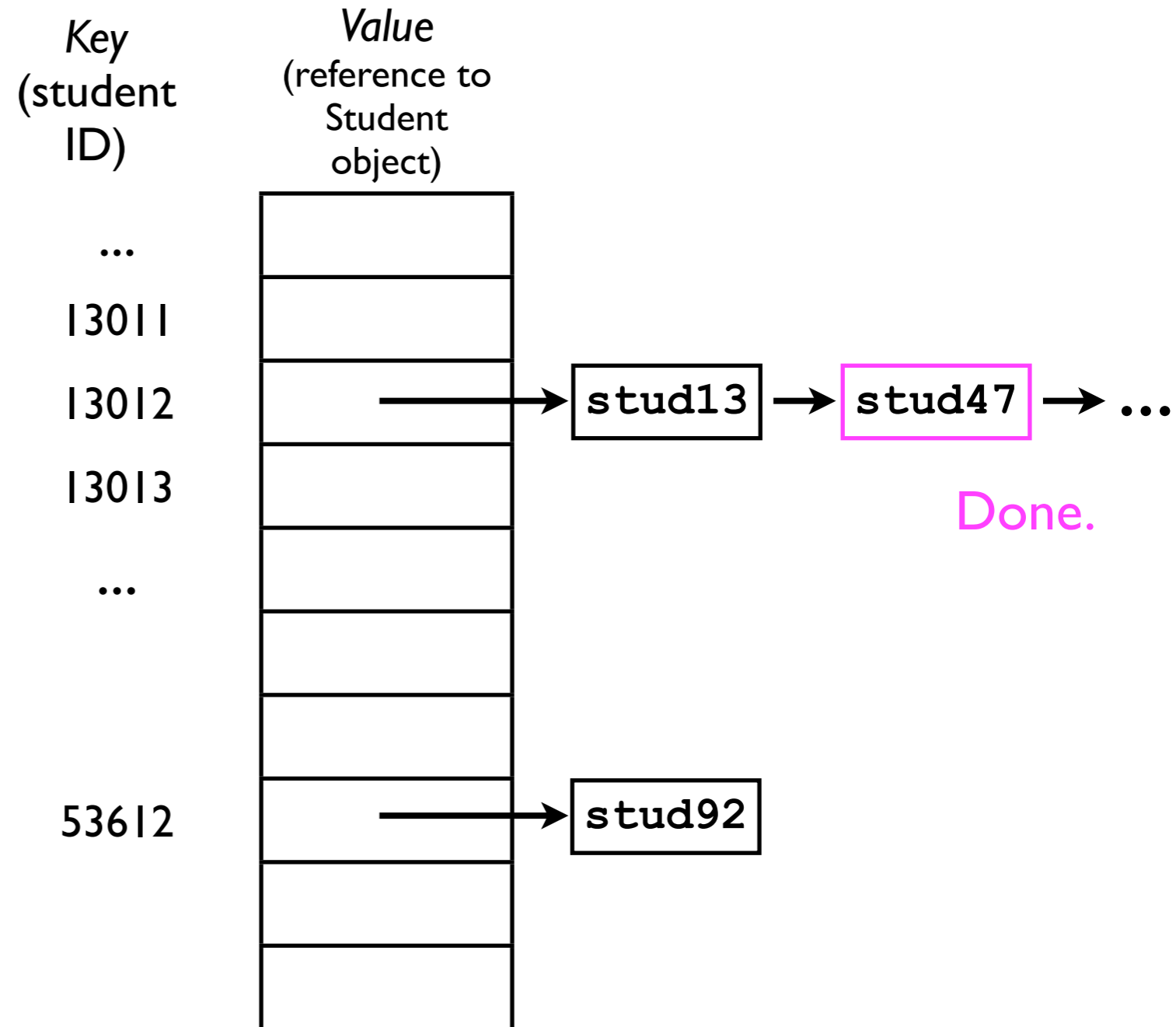
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Chaining

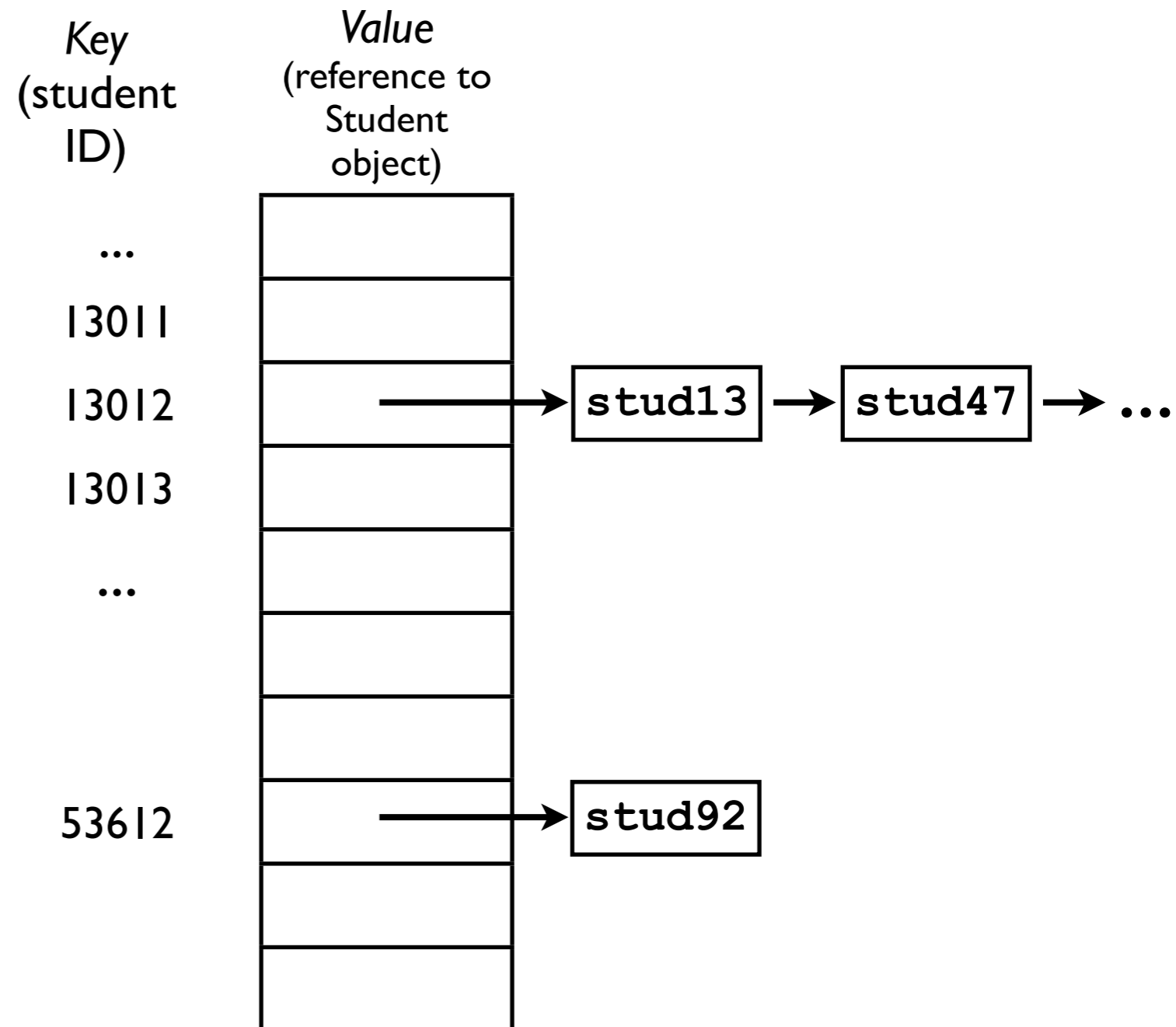
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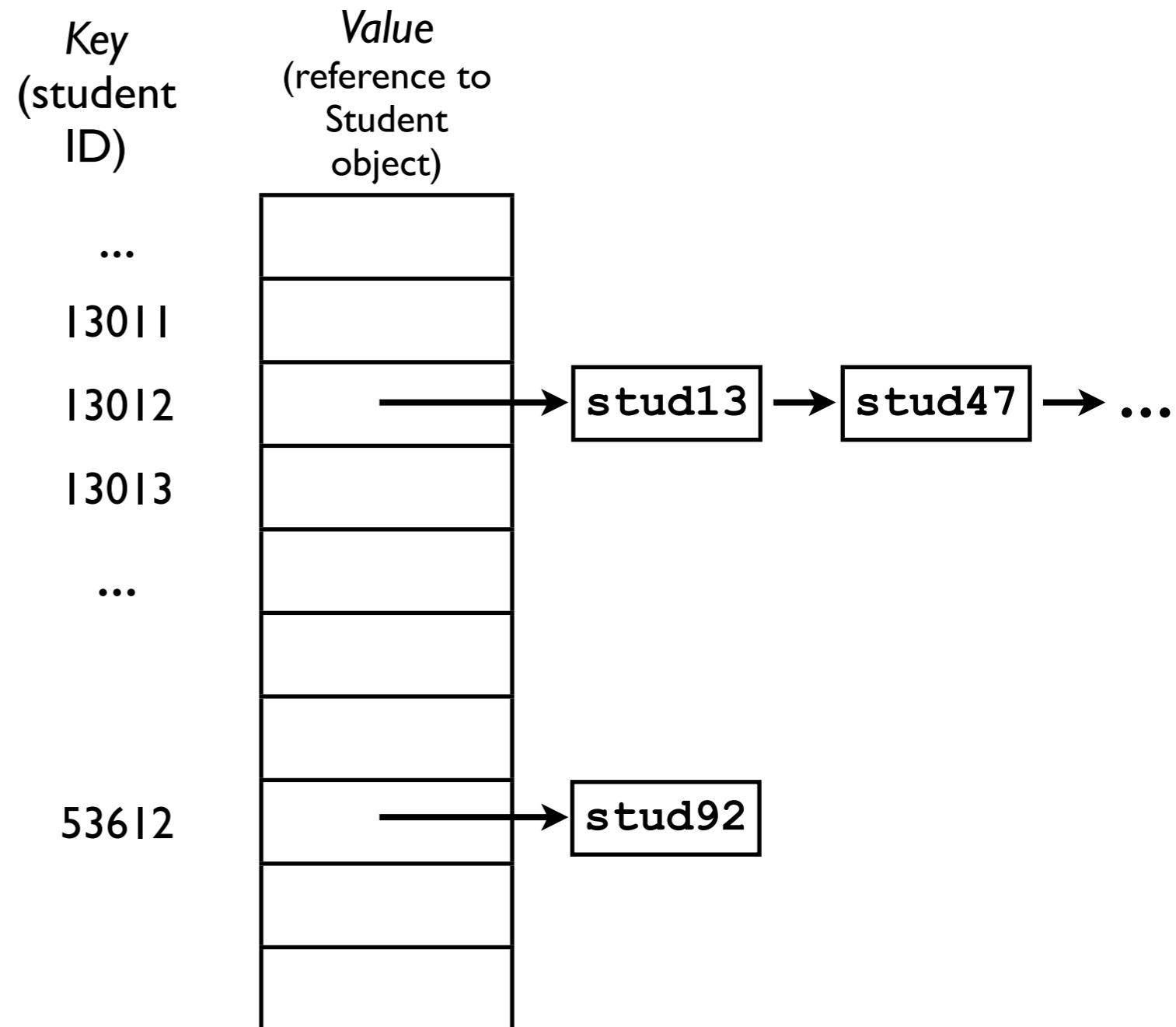
Chaining

- If we reach the end of the linked list and don't find the desired student, then we know that student is *not contained in the hash table*.
- There is *no other slot* at which the Student object would be stored.



Chaining

- If we wish to *remove* a student (e.g., `stud13`), we just:
 1. Hash the student ID of the student we want to remove.
 2. Find that student in the linked list.
 3. “Splice it out”.



Chaining:

Performance analysis

- How fast are the `add/remove/find` operations for a hash table with chaining?
- To find an object in a hash table, we must:
 - Hash the key. $O(1)$
 - Jump to that array index. $O(1)$
 - Traverse through the linked list at that index. $O(?)$

Chaining:

Performance analysis

- In the *worst case*, all N objects stored in the hash table will hash to the *same array index*.
- This means that the linked list at that index will be N elements long.
 - To find an arbitrary element in a linked list we need $O(n)$ time.
 - This is no better than just using a linked list by itself!

Chaining: Performance analysis

- However, in the *average* case, a hash table performs much better:
 - Given M slots and N actual objects stored, the average list length for any array slot is N/M .
 - Then, the average time to access any arbitrary object is $O(1 + N/M)$.
 - Now, suppose that we always make sure that $M > N$.
 - Then $N/M < 1$.
 - Hence, average-case time cost is $O(1 + N/M) = O(1)$.

Open addressing

- An alternative to *chaining* is *open addressing*.
- With *open addressing*, there are no linked lists associated with array slots.
- Instead, if a given slot is already “full”, then the hash table “tries another one”.
- There are different strategies for “finding another one”.
- Confusingly, open addressing is sometimes also known as *closed hashing*:
 - The “closed” refers to the fact that all data are stored within the array itself, not in a separate chain.

Open addressing

- There are different strategies for “finding another slot”:
 - Simplest -- **linear probing**:
 - If `hashFunction(key)` maps into an index i that is already occupied, then try $i+1$.
 - If that doesn't work, try $i+2, i+3, \dots$, etc.
 - If we get to $M-1$, we want to “wrap around” back to 0.
 - The index of the j th probe (where j starts at 0) is given by the expression:

$$(i+j) \% M$$

Open addressing

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 - If we get to $M-1$, we want to “wrap around” back to 0.
 - The index of the j th probe (where j starts at 0) is given by the expression:

$$(i+j) \% M$$

Why not $(i \% M) + j$?

Open addressing

- Linear probing is simple to implement. However, it will tend to cause large amounts of *clustering* (more later).
- Better performance is achieved by **quadratic probing**:
- If `hashFunction(key)` maps into an index i , then the index of the j th probe is given by the expression:

$$(i + c_0*j + c_1*j^2) \% M$$

Linear probing

- Suppose our hash table contains $M=100000$ buckets, and we wish to add `student2` to the hash table, and `hashFunction(studentID2)` returns `13011`.
- This slot is occupied by `student1`.
- The next slot we try is $(13011+1) \% 100000 = 13012$.
- Since `13012` is available, we can insert `student2` at that slot.

Key (student ID)	Value (reference to Student object)
...	
13011	student1
13012	
13013	
...	
53612	

Linear probing

- Suppose our hash table contains $M=100000$ buckets, and we wish to add `student2` to the hash table, and `hashFunction(studentID2)` returns `13011`.

- This slot is occupied by `student1`.

- The next slot we try is $(13011+1) \% 100000 = 13012$.

- Since `13012` is available, we can insert `student2` at that slot.

Key (student ID)	Value (reference to Student object)
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13011	student1
13012	
13013	
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- This slot is occupied by `student1`.
- The next slot we try is $(13011+1) \% 100000 = 13012$.
- Since `13012` is available, we can insert `student2` at that slot.

Key (student ID)	Value (reference to Student object)
...	
13011	student1
13012	
13013	
...	
53612	

Linear probing

- Suppose our hash table contains $M=100000$ buckets, and we wish to add `student2` to the hash table, and `hashFunction(studentID2)` returns `13011`.
 - This slot is occupied by `student1`.
 - The next slot we try is $(13011+1) \% 100000 = 13012$.
 - Since `13012` is available, we can insert `student2` at that slot.

Key (student ID)	Value (reference to Student object)
...	
13011	student1
13012	student2
13013	
...	
53612	

Linear probing

- When we later wish to find `student2`, we:

1. Compute its index using the hash function ($i = |3011|$).
2. Search down the array (using linear probing) until we find the correct object, *or* until we find an empty slot.
 - If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Linear probing

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...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
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Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
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13013	
...	
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Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

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- If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	student1
13012	student2
13013	
...	
53612	

Done.

Linear probing

- Suppose we search for `student9`, whose hash code happens to also be 13011:

1. Compute its index using the hash function ($i=13011$).
2. Search down the array (using linear probing) until we find the correct object, *or* until we find an empty slot.
 - If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Linear probing

- Suppose we search for `student9`, whose hash code happens to also be `13011`:

1. Compute its index using the hash function ($i=13011$).

2. Search down the array (using linear probing) until we find the correct object, *or* until we find an empty slot.

- If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Linear probing

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 2. Search down the array (using linear probing) until we find the correct object, or until we find an empty slot.
- If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Linear probing

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Key (student ID)	Value (reference to Student object)
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13011	<code>student1</code>
13012	<code>student2</code>
13013	
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Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
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Linear probing

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2. Search down the array (using linear probing) until we find the correct object, *or* until we find an empty slot.

- If we find an empty slot, then we know `student2` is *not* contained in the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Open addressing

- Open addressing requires less memory than chaining because there are no linked lists.
- However, they suffer from a few complications:
 1. Removing an element.
 2. Clustering.

Key (student ID)	Value (reference to Student object)
...	
13011	student1
13012	student2
13013	
...	
53612	

Removing an element

- Suppose we remove `student1` from the hash table.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student1</code>
13012	<code>student2</code>
13013	
...	
53612	

Removing an element

- Suppose we remove `student1` from the hash table.
- If we later search for `student2`, we will still hash to 13011, but find that it is *empty*.
- Does that mean `student2` is not contained in the hash table?
- No -- but we have to *record* that somehow.

Key (student ID)	Value (reference to Student object)
...	
13011	
13012	<code>student2</code>
13013	
...	
53612	

Removing an element

- One method of recording that an element was deleted is a *bridge*, a special element that indicates “empty, but keep looking.”
- If we later add another element, say `student5` that hashes to `13011`, then we can *replace* the bridge with a real `Student` object.

Key (student ID)	Value (reference to Student object)
...	
13011	(bridge)
13012	<code>student2</code>
13013	
...	
53612	

Removing an element

- One method of recording that an element was deleted is a *bridge*, a special element that indicates “empty, but keep looking.”
- If we later add another element, say `student5` that hashes to `13011`, then we can *replace* the bridge with a real `Student` object.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student5</code>
13012	<code>student2</code>
13013	
...	
53612	

Clustering

- The other downside of open addressing is **clustering**.
- If too many keys hash to the same index -- *or to nearby indices* -- then the linear probing may become expensive.
- Consider the hash table to the right:
 - 13011-13016 are already occupied.
 - If we want to add another student `student7` who also hashes to 13011, then we have to step through 7 elements.
 - The longer the cluster, the higher the time cost for add/find/remove.

Key (student ID)	Value (reference to Student object)
...	
13011	<code>student5</code>
13012	<code>student1</code>
13013	<code>student9</code>
13014	<code>student8</code>
13015	<code>student3</code>
13016	<code>student4</code>
13017	
...	

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- If too many keys hash to the same index -- *or to nearby indices* -- then the linear probing may become expensive.
- Consider the hash table to the right:
 - 13011-13016 are already occupied.
 - If we want to add another student **student7** who also hashes to 13011, then we have to step through 7 elements.
 - The longer the cluster, the higher the time cost for add/find/remove.

Key (student ID)	Value (reference to Student object)
...	
13011	student5
13012	student1
13013	student9
13014	student8
13015	student3
13016	student4
13017	student7
...	

Open addressing

- Like chaining, *open addressing* guarantees $O(1)$ time cost for the add/find/remove operations *so long as* $M > N$.
- Due to the bridging complication, open addressing is most useful when elements will *never be deleted*.
- The memory saved by not using linked lists can be used to allocate more slots \implies higher M .
- The larger M is, the fewer collisions will occur, and the better the average-case performance will be.

Hash table ADTs

- So far we've focused more on how a hash table is implemented *internally* and less how a user would *use* it.
- There are two different *interfaces* that a hash table ADT might offer.
- The interface varies depending on whether:
 1. Key is a field *inside* the whole record.
 2. Key is *separate* and stored *outside* the record.

Key inside the record

- In some previous code examples we've conceptualized the *key* as a *field* within the whole object, e.g.:

```
class Student {  
    int _studentID;  
    String _firstName, _lastName;  
    boolean _hasTeddyBear;  
}
```

- This implementation of *keys* then lends itself to the following hash table interface:

```
interface HashTable<T extends HasKey> {  
    void add (T o);  
    T get (T o);  
}
```

where the hypothetical **HasKey** interface guarantees that **T** offers a method called `int getKey()`.

Key inside the record

- The `HashTable` then might then be implemented as:

```
class HashTableImpl<T extends HasKey>
implements HashTable<T> {

    T[] _array;
    ...
    void add (T o) {
        _array[hashFunction(o.getKey())] = o;
    }

    T get (T o) {
        return _array[hashFunction(o.getKey())];
    }
}
```

Key inside the record

- The user could then use the hash table as follows:

```
class Student implements HasKey {
    int _studentID;
    String _firstName, _lastName;
    boolean _hasTeddyBear;
    ...
    int getKey () {
        return _studentID;
    }
}
```

```
hashTable<Student> students = new HashTable<Student>();
```

```
students.add(new Student(12345, "Jacky", "O'Nassis"));
```

```
students.add(new Student(9231, "Bette", "Midler"));
```

```
...
```

```
Student someStudent = students.get(new Student(9231));
```

Key inside the record

- It turns out this hypothetical `HasKey` interface is unnecessary because the `Java Object` class already offers a `hashCode ()` method.
- `hashCode ()` should return some “integer representation” of the object.
- The default implementation of `Object.hashCode ()` is simply to return the *address* in memory (an `int`) of the object.
- Subclasses of `Object` can override `hashCode ()` to do something more meaningful.

hashCode ()

- For example, we could override hashCode () in Student to return the Student's _studentId field:

```
class Student implements HasKey {  
    int _studentID;  
    String _firstName, _lastName;  
    boolean _hasTeddyBear;  
    ...  
    public int hashCode () {  
        return _studentID;  
    }  
}
```

← HasKey interface no longer necessary

hashCode ()

- Because hashCode () is available in every *Java Object*, we can simplify both the interface and implementation of the `HashTable<T>`:

```
interface HashTable<T extends HasKey> {  
    void add (T o);  
    T get (T o);  
}  
  
class HashTableImpl<T> implements HashTable<T> {  
    ...  
    void add (T o) {  
        _array[hashFunction(o.hashCode())] = o;  
    }  
  
    T get (T o) {  
        return _array[hashFunction(o.hashCode())];  
    }  
}
```

← `HasKey` interface no longer necessary

Non-integer keys

- `hashCode ()` also provides useful functionality for supporting *non-integer keys*.
- E.g., we want to use a `Student`'s full name as the key.
 - A name is a `String`, which is not an `int`.
 - How do we convert from a `String` into an (`int`) index into the hash table?
 - Just delegate to `String.hashCode ()`.

Non-integer keys

- Example:

```
class Student {
    int _studentID;
    String _firstName, _lastName;
    boolean _hasTeddyBear;
    ...
    public int hashCode () {
        String fullName = _firstName + " " + _lastName;
        return fullName.hashCode();
    }
}
```

Since `fullName` is a `String`, and `String` is an `Object`, then `fullName` is guaranteed to support the `hashCode()` method.

Hash code examples

- Suppose our key is:
 - A single character `c`:
 - We could convert `c` into its ASCII value, which is an integer (from 0-127).
 - A `String s` of characters:
 - We could convert each `c` in `s` to its ASCII value, and then add them together.
 - An image `im`:
 - We could add together the pixel values across all three (R,G,B) channels.

Note: these are just hypothetical examples, not necessarily how Java actually implements hash codes!

hashCode ()

- In Java, the `hashCode ()` method *must* uphold two properties:
 - I. *Deterministic* -- multiple subsequent calls to `hashCode ()` on the *same object* `o` must return the same value.
- Otherwise, `hashFunction (key.hashCode ())` would map into a different array index -- and the hash table wouldn't be able to find `o`.

```
_array[hashFunction(o.hashCode ())] = o;    // Add  
...  
return _array[hashFunction(o.hashCode ())]; // Find
```

hashCode ()

2. *Consistent across equal instances* -- if `o1.equals(o2)`, then `o1.hashCode()` *must* equal `o2.hashCode()`:

```
String s1 = "hello";  
String s2 = new String("hello"); // Distinct copy  
int hashCode1 = s1.hashCode();  
int hashCode2 = s2.hashCode(); // Must equal hashCode1
```

- This means that if class **A** overrides the `equals()` method, then it must also override `hashCode()`.

hashCode ()

- In addition, it is *desirable* for hashCode () to have:
 3. *Wide distribution across instances* -- hashCode () should return *different* values for *different* instances of the same class as much as possible.
- If `A.hashCode ()` returned the *same* hash value for every instance `o`, then *all* objects of type `A` would map into the same array index. `hashCode ()` is always the same.

```
_array[hashFunction(key1.hashCode ())] = o1;  
_array[hashFunction(key2.hashCode ())] = o2; // Collision  
_array[hashFunction(key3.hashCode ())] = o3; // Collision  
_array[hashFunction(key4.hashCode ())] = o4; // Collision
```

- This would yield terrible ($O(n)$) hash performance!

Key outside the record

- More commonly, however, hash tables *separate* the key from the *value*.
- A typical hash table interface might be:

```
interface HashTable<K, V> {  
    void put (K key, V value);  
    V get (K key);  
}
```

Here, we are defining *two different* type parameters K (for keys) and V (for values).

Key outside the record

- This may be more convenient than the `HashTable` interface where the key is inside the record.

- Compare:

- Key inside record:

```
hashTable.add(new Student(123, "Jimmy", "Carter"));  
...  
Student student = hashTable.get(new Student(123));
```

- Key separate from record:

```
hashTable.put(123, new Student("Jimmy", "Carter"));  
...  
Student student = hashTable.get(123);
```

No need to instantiate new `Student` object just to find an existing one.

Key outside the record

- Separating keys from values is especially useful when we use a hash table as a *dictionary*.
- A **dictionary** is a data structure for storing a set of associations between keys and values.

Key outside the record

- Example:
- We can create a dictionary of English words to their meanings:

```
HashTable<String,String> englishDictionary =  
    new HashTable<String,String>();  
englishDictionary.put(  
    "eggplant",  
    "The somewhat large egg-shaped fruit of a  
    tropical Old World plant, eaten as a vegetable."  
);  
  
...  
  
String meaning = englishDictionary.get("eggplant");
```

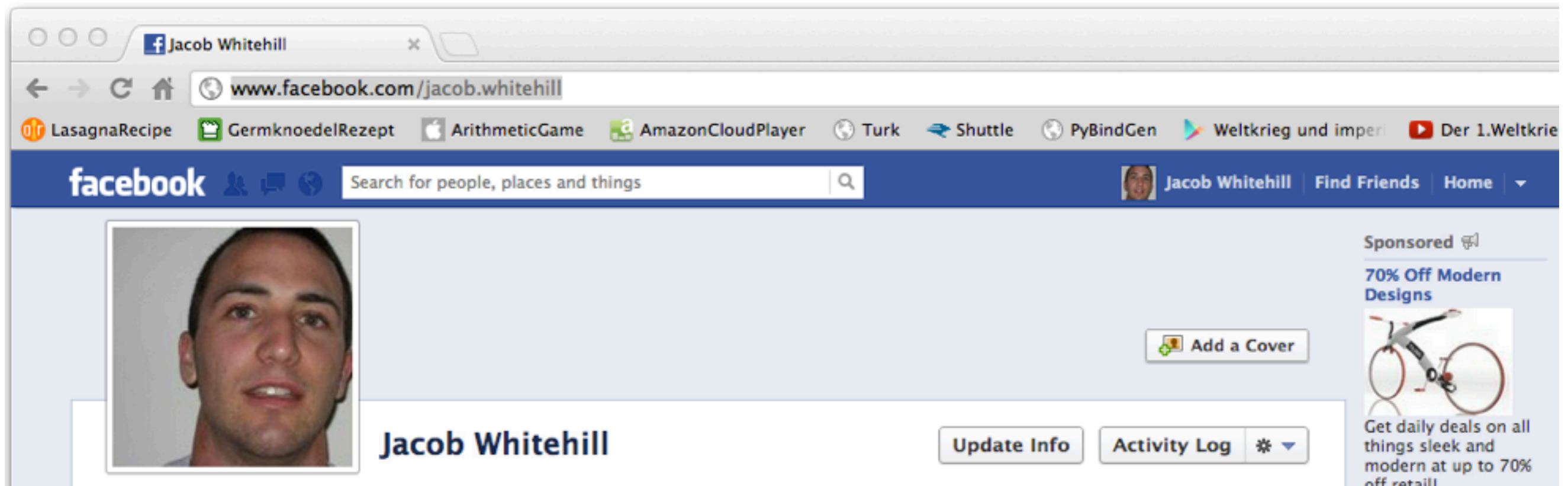
Key outside the record

- To implement a `HashTable` in which keys are stored separately from values, we must “bind” the key and value together inside the table:

```
class HashTableImpl<K,V> implements HashTable<K,V> {
    static class Bucket {
        K _key;
        V _value;
        ...
    }
    Bucket[] _array;
    ...
    void put (K key, V value) {
        int bucketIdx = hashFunction(key.hashCode());
        _array[bucketIdx]._key = new Bucket(key, value);
    }

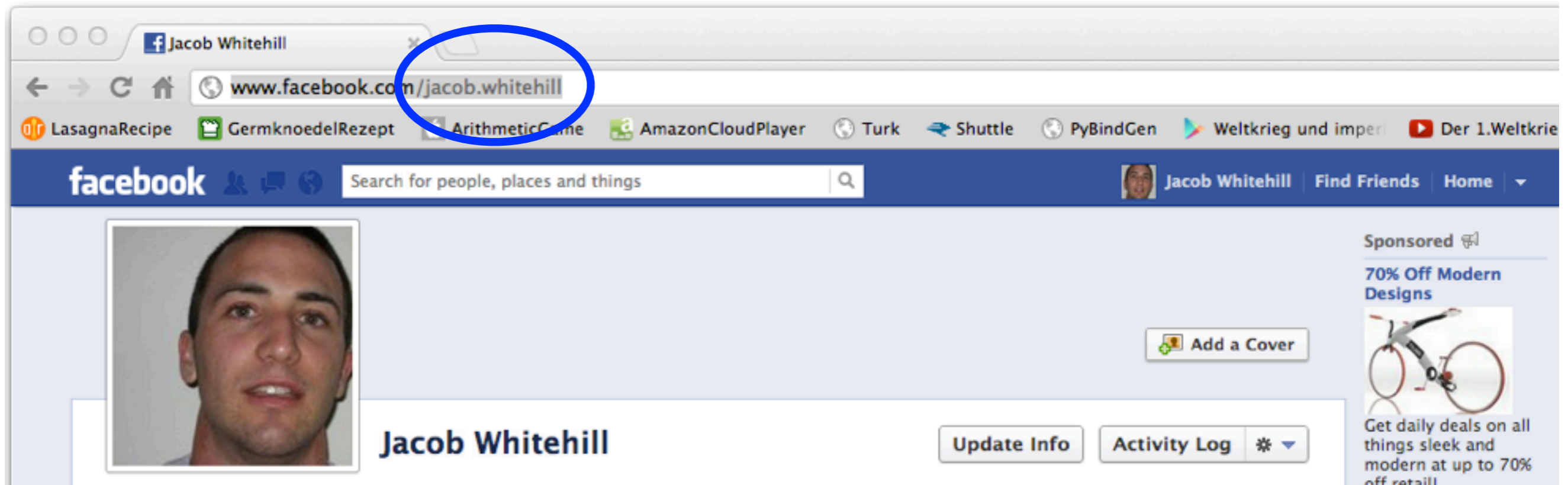
    V get (Key key) {
        return _array[hashFunction(key.hashCode())]._value;
    }
}
```

Hash table usage example



- Suppose we were implementing the Web server for Facebook.
- Server must be robust to handle **billions** of requests per day!

Hash table usage example



- Facebook access is initiated when user enters the **username** of a particular user.
- Given the username, the Facebook page, including pictures and text, must be found **fast**.

Hash table usage example

- Possible implementation:

```
Image findUserProfilePicture (String username) {  
    String pathToImageFile = _usersToImagePaths.get(username) ;  
    return new Image(pathToImageFile) ;  
}
```

This needs to be super-fast to handle Facebook's typical load; hence, use a **hash table**.